

THEORY OF COMPUTATION

DEPARTMENT OF COMPUTER ENGINEERING

Subject : TOC

ASSIGNMENT NO – 03

Unit : III

THEORY QUESTION

1. Write in brief about “**Sentential form**” with reference to context free Grammar
2. Explain with suitable examples, any **two applications of Context Free Grammar.**
3. Discuss **applications of Context Free Grammar in XML.**
4. Discuss applications of Context Free Grammar in **Syntax Analysis of a Compiler.**
5. What are the different types of **Normal Forms of Context Free Grammar?**
Explain it with example
6. Write short notes on 1. **CNF** 2. **GNF**

CONTEXT FREE GRAMMAR(CFG)

1. Construct the Context Free Grammar for the language having **any number of a's** over the set $\Sigma = \{a\}$.
2. Write the grammar generating all **strings consisting of a's and b's with at least two a's.**
3. **Write context free grammar** for the following language
 - I. $0(0+1)^* 01(0+1)^* 1$
 - II. $(a+b)^* bbb (a+b)^*$
4. **Write the CFG for following language.**
 $L = \{a^{m+n} b^m c^n | n, m \geq 0\}$
5. **Write CFG for following Language.**
 $L = \{a^n b^m a^n | n \geq 0, m \geq 1\}$
6. Describe the language L for given **Context Free Grammar** $G = [\{S\}, \{a,b\}, P, \{S\}]$
where $P = \{S \rightarrow aSb, S \rightarrow ab\}$.

7. Write CFG for the following languages.

$$L = \{0^i 1^j 0^k \mid j > i + k\}$$

$$L = \{0^i 1^j 2^k \mid i = j + k\}$$

Write CFGs for given CFLs : [8]

- i) Languages containing the strings with equal number of a's and b's
- ii) Languages containing the strings containing a's and b's with at least 2 a's

Give context free grammars for the following languages: [6]

- i) $L = \{x \mid x \in \{(\cdot)\}^* \text{ with strings having well-formed parentheses (WFP)}\}$
- ii) $L = \{a^m b^n c^{m+n} \mid m, n \geq 0\}$

Write the CFG for language $L = \{0^i 1^j 0^k \mid j > i + k\}$.

Show the derivation of the string '0111100'.

SIMPLIFY/ELIMINATE GRAMMAR

1. Simplify the grammar:

$S \rightarrow Ab, A \rightarrow a, B \rightarrow C|b, C \rightarrow D, D \rightarrow E, E \rightarrow a$

2. Eliminate ϵ -productions from the grammar G

$A \rightarrow aBb|bBa$

$B \rightarrow aB|bB|\epsilon$

3. Optimize the CFG given below by reducing the grammar where S is a start symbol.

$S \rightarrow A | 0C1$

$A \rightarrow B | 01 | 10$

$C \rightarrow \epsilon | CD$

4. Consider the grammar $G = \{(A, B), (a, b), P, A\}$ where P consists of

$A \rightarrow B$

$B \rightarrow a|b$

Eliminate unit productions

5. Simplify the following Context Free Grammar (CFG).

$$S \rightarrow ASB \mid \epsilon$$

$$A \rightarrow aAS \mid \epsilon$$

$$B \rightarrow Sbs \mid A \mid bb$$

$G = \{(S,A,B), (a,b), S,P : \text{Productions are given above}\}$

Simplify the following grammar

i) $S \rightarrow Ab, A \rightarrow a, B \rightarrow C \mid b, C \rightarrow D, D \rightarrow E, E \rightarrow a$

ii) $S \rightarrow 0A0 \mid 1B1 \mid BB, A \rightarrow C, B \rightarrow S \mid A, C \rightarrow S \mid \epsilon$

LEFT LINEAR AND RIGHT LINEAR GRAMMAR

1. Write an equivalent **right linear grammar** for following **left linear grammar**

$$S \rightarrow SI0 \mid 0.$$

2. Write equivalent left linear grammar for the following right liner grammar.

$$S \rightarrow 0A$$

$$A \rightarrow 10A \mid C$$

3. Write an equivalent left-linear grammar for the right-linear grammar.

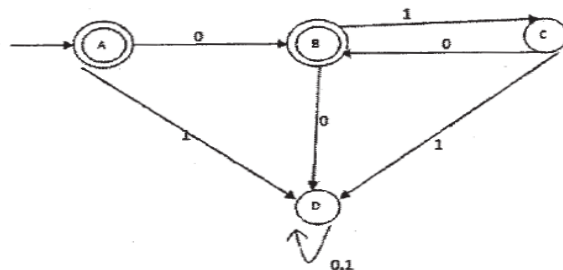
$$S \rightarrow 0A \mid B$$

$$A \rightarrow 0C \mid 1A \mid 0$$

$$B \rightarrow 1B \mid 1A \mid 1$$

$$C \rightarrow 0 \mid 0A$$

Give the Right & Left linear grammar for the following DFA shown in Fig1 [8]



Construct a DFA for the following left linear grammar

$$S \rightarrow B1 \mid A0 \mid C0, \quad B \rightarrow B1 \mid 1, \quad A \rightarrow A1 \mid B1 \mid C0 \mid 0, \quad C \rightarrow A0$$

CFG, CNF and GNF

1. Convert following CFG to CNF.

$$S \rightarrow AACD$$

$$A \rightarrow aAb | \epsilon$$

$$C \rightarrow aC | a$$

$$D \rightarrow aDa | bDb | \epsilon$$

2. Write CFL for following CFG

$$S \rightarrow aB | bA$$

$$A \rightarrow a | aS | bAA$$

$$B \rightarrow b | bS | Abb$$

3. Convert the following grammar to GNF

$$S \rightarrow ABA | AB | BA | AA | A B$$

$$A \rightarrow aAa$$

$$B \rightarrow bB | b$$

4. Convert the following grammar to CNF.

$$S \rightarrow bA | aB$$

$$A \rightarrow bAA | as | a$$

$$B \rightarrow aBB | bs | b$$

5.

Convert the following CFG into Chomsky Normal Form (CNF):

$$S \rightarrow AB$$

$$A \rightarrow CA | \wedge$$

$$B \rightarrow DB | \wedge$$

$$C \rightarrow 011 | 1$$

$$D \rightarrow 01$$

6.

Check whether the given grammar is in CNF. If not then find its equivalent CNF. [8]

$$S \rightarrow bA | aB, A \rightarrow bAA | aS | a, B \rightarrow aBB | bS | b$$

*****THE END*****