

# THEORY OF COMPUTATION

## DEPARTMENT OF COMPUTER ENGINEERING

Subject : TOC

ASSIGNMENT NO – 04

Unit : IV

### THEORY QUESTION

1. Define **PDA**. What are different types of PDA? Applications of PDA?
2. Prove that "Let L be a language accepted by **deterministic PDA**, then the complement of L, can also be accepted by, deterministic PDA
3. Proves the **CFL are Closed under Union**, Concatenation and Kleene's closure.
4. Show that **CFL are closed under intersection** and Complementation.
5. Explain the working of **top down parser** and **bottom up parser** with example.
6. Differentiate between **FA and PDA**.
7. What are different ways to define PDA Acceptability
8. Explain acceptance by **PDA**
  - i ) By Final State
  - ii ) By Empty state

Construct PDA that accepts all palindrome string over {a, b} . Specify simulation for string 'aba'.
9. **Explain Closure property of PDA** with suitable example.

### POSTDOWN AUTOMATA (PDA)

10. Construct **PDA** that accepts the language by the following CFG.  $S \rightarrow SS \mid (S) \mid ()$
11. Design a PDA for accepting a language  $L = \{a^n b^m c^n \mid m, n \geq 1\}$
12. Design a PDA for accepting Language  $L = \{W c W^R \mid W \in (a,b)^*\}$ .
13. Construct **PDA** that accepts following language  $L = \{a^n b^n \mid n \geq 0\}$ . Write simulation for string 'aaabbb'
14. Design a **PDA** for the following Language  $L = \{a^n b^{2n} \mid n \geq 0\}$
15. Show that:  $L = \{a^n b^n c^n \mid n \geq 1\}$  not a CFL
16. Design a **PDA** for the following Language  $L = \{a^{2n} b^n \mid n \geq 1\}$  n=3

**POST MACHINE (PM)**

17. What is **Post Machine**? Give formal definition of Post Machine. Construct a Post Machine for accepting strings with equal number of a's and b's.

18. Construct **post machine** that accepts following language

$$L = \{a^n b^m \mid n \geq 0, m \geq 0\}$$

19. 13. Construct **post Machine** that accepts the following language.

$$L = \{a^n b^n a^n \mid n \geq 0\}$$

**CFG TO PDA**

20. Convert following **CFG to PDA**

$$S \rightarrow aSb \mid A$$

$$A \rightarrow bSa \mid S \mid \epsilon$$

21. **Construct PDA** for the following Regular Grammar :

$$S \rightarrow 0A \mid 1B \mid 0$$

$$A \rightarrow A0 \mid B$$

$$B \rightarrow c \mid d$$

**NPDA**

22.

What is NPDA? Construct a NPDA for  $L = \{a^i b^j c^k \mid i \neq j \text{ or } j \neq k\}$

23.

Construct a NPDA that accepts the language  $L = \{a^n \mid n > 0\}$

24.

What is NPDA? Construct a NPDA for The set of all strings over  $\{a,b\}$  with even length palindrome. [10]

25. Construct the **NPDA** that accepts the language generated by

$$S = S + S \mid S * S \mid 4$$

### PDA TO CFG

26.

Give Context Free Grammar (CFG) generating the language accepted by the PDA  $M = \{(q_0, q_1), (a, b), \delta, q_0, Z_0, q_1\}$  where  $\delta$  is as follows.

1.  $(q_0, a, Z_0) \rightarrow (q_0, XZ_0)$
2.  $(q_0, a, X) \rightarrow (q_0, XX)$
3.  $(q_0, b, X) \rightarrow (q_1, \epsilon)$
4.  $(q_1, b, X) \rightarrow (q_1, \epsilon)$
5.  $(q_1, \epsilon, Z_0) \rightarrow (q_1, \epsilon)$

27.

Obtain the CFG for the PDA given by  $M = \{\{q_0, q_1\}, \{0, 1\}, \{z_0, X\}, \delta, q_0, z_0, \phi\}$  where  $\delta$  is given as. [9]

$$\delta(q_0, 1, z_0) = \{q_0, xz_0\} \quad \delta(q_0, 1, x) = \{q_0, xx\}$$

$$\delta(q_0, 0, x) = \{q_1, x\} \quad \delta(q_0, \epsilon, z_0) = \{q_0, \epsilon\}$$

$$\delta(q_1, 1, x) = \{q_1, \epsilon\} \quad \delta(q_0, 1, z_0) = \{q_0, z_0\}$$

28.

Obtain CFG for the PDA given below:

$$\delta(q_0, 1, z_0) = \{q_0, xz_0\} \quad \delta(q_0, 1, x) = \{q_0, xx\}$$

$$\delta(q_0, 0, x) = \{q_1, x\} \quad \delta(q_0, \epsilon, z_0) = \{q_0, \epsilon\}$$

$$\delta(q_1, 1, x) = \{q_1, \epsilon\} \quad \delta(q_0, 1, z_0) = \{q_0, z_0\}$$

29.

Give a grammar for the language  $L(M)$ , where:  
 $M = (\{q_0, q_1\}, \{0, 1\}, \{z_0, X\}, \delta, q_0, z_0, \Phi)$ .  
 And  $\delta$  is given by:

$$\delta(q_0, 1, z_0) = (q_0, xz_0) \quad \delta(q_0, \epsilon, z_0) = (q_0, \epsilon)$$

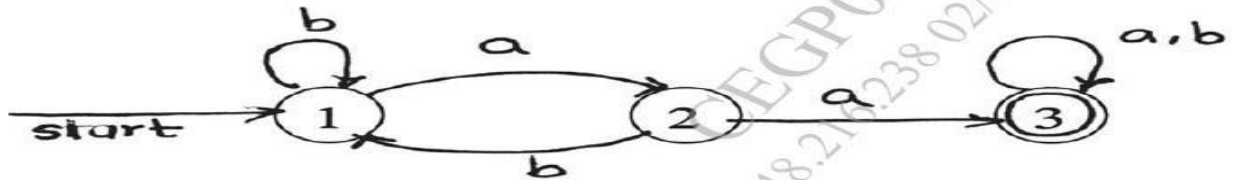
$$\delta(q_0, 1, x) = (q_0, xx) \quad \delta(q_1, 1, x) = (q_1, \epsilon)$$

$$\delta(q_0, 0, x) = (q_1, x) \quad \delta(q_0, 0, z_0) = (q_0, z_0)$$

**MISCELLNEOUS EXAMPLES**

30.

Construct a PDA that recognizes the language accepted by following DFA. [6]



31.

Illustrate the working of Shift Reduce parser for  $id+id*id$ .

Consider the following grammar:

$$E \rightarrow E + E \mid T$$

$$T \rightarrow T * F \mid F$$

$$F \rightarrow \{E\} \mid id$$

\*\*\*\*\*THE END\*\*\*\*\*